

More Quadratic Graphs & Second Differences

Problem 1:

A football is thrown into the air from a height of 6 feet with an initial vertical velocity of 50 feet per second. The function $g(t) = -16t^2 + 50t + 6$ represents the height of the football, $g(t)$, t seconds after it was thrown.

1. What is the y-intercept? What does it represent in the scenario?

$(0, 6)$ the initial height of the football.
the football starts at a height of 6 ft.

2. What are the x-intercepts? What do they represent in the scenario?

$(-0.12, 0)$ has no meaning in the problem, because time can't be negative.
 $(3.2, 0)$ 3.2 is the time it takes to reach a height of 0. (hit the ground)

3. What is the turning point? Is the turning point a minimum or maximum?

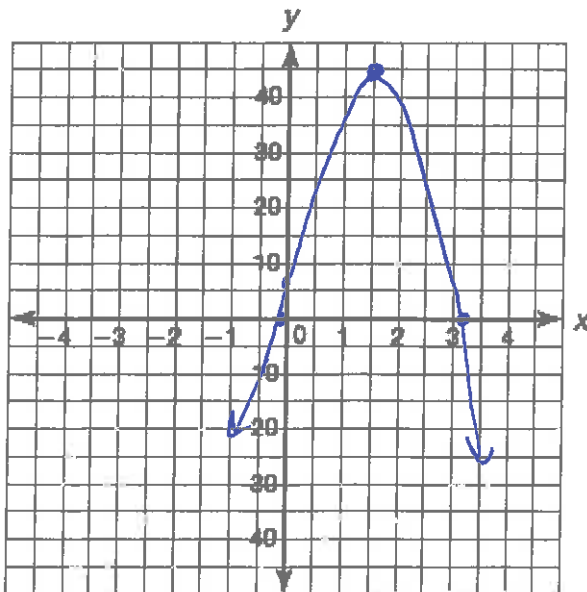
$(1.5, 45)$ is a maximum.

4. Zeros – The x-coordinate of the x-intercepts. They are the same as the Roots.

What are the zeros of the quadratic?

$x = -0.12$ and $x = 3.2$

5. Use the intercepts and turning point to graph the quadratic on the grid below.



Problem 2: Interval Notation

Use "[" or "]" to represent a filled in circle (\leq or \geq).

Use "(" or ")" to represent an open circle ($<$ or $>$).

1. Use interval notation to represent each described interval.

a. All real numbers greater than 4, but less than or equal to 10.



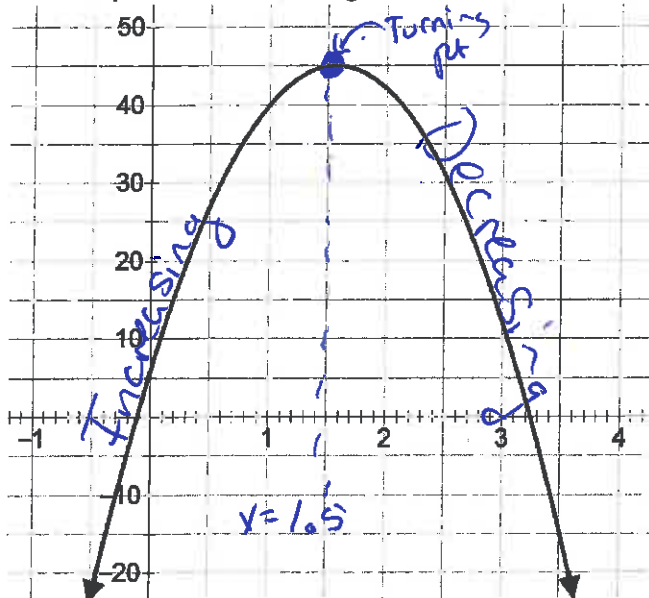
b. All real numbers less than or equal to 8.



c. All real number greater than -2 and less than 0.



2. Give your answers using interval notation.



a. What is the domain of the function?

Domain is all real numbers (x-values)
 $(-\infty, \infty)$

b. What is the range of the function?

Range (y-values) are all real #'s less than or equal to 45.
 $(-\infty, 45]$

c. Over what interval is the function increasing?

$(-\infty, 1.5)$

d. Over what interval is the function decreasing?

$(1.5, \infty)$

Problem 3: Second Differences

You can distinguish a linear table of values from a quadratic table of values by analyzing the first and second differences.

First, make sure that the x values all increase by 1.

First Differences – Subtract consecutive y values.

Second differences – Subtract consecutive first differences.

x	y	First Differences	Second Differences
-1	10		
0	8	-2	0
1	6	-2	0
2	4	-2	0
3	2	-2	0

Handwritten calculations and arrows:
 $4 - 6 = -2$
 $2 - 4 = -2$

Linear Functions will have **constant First Differences and 0 Second Differences**

Quadratic Functions will have **changing First Differences and constant Second Differences.**

1. Does the table above represent a linear or quadratic function?

Linear function.

2. Describe the type of function represented in the table, based on the first and second differences.

a.

x	y	First Differences	Second Differences
-2	-6		
-1	-3	3	0
0	0	3	0
1	3	3	0
2	6	3	0

Linear

b.

x	y	First Differences	Second Differences
-1	1		
0	0	-1	4
1	3	3	4
2	10	7	4
3	21	11	4

Quadratic

